



Unified International
Mathematics Olympiad

UNIFIED INTERNATIONAL MATHEMATICS OLYMPIAD

CLASS - 7

Question Paper Code : 4P104

KEY

| | | | | | | | | | |
|---------|---------|---------|-----|-------|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| A | C | A | A | A | A | A | B | A | A |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| A | B | B | A | D | A | D | C | D | C |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| D | A | C | B | B | D | A | B | D | C |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| A,B,C,D | A,B,C,D | A,B,C,D | B,C | B,C,D | B | C | D | C | C |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| D | B | B | D | A | B | D | A | D | D |

SOLUTIONS

MATHEMATICS – 1 (MCQ)

01. (A) Area = $9 \times 1 \text{ cm}^2 + 7 \times 1 \text{ cm}^2 + 5 \times 1 \text{ cm}^2 = 21 \text{ cm}^2$

02. (C) Given $n \parallel t$
 $\Rightarrow a + 70^\circ = 180^\circ \Rightarrow \angle a = 110^\circ$
 $l \parallel m \Rightarrow b + 130^\circ = 180^\circ \Rightarrow \angle b = 50^\circ$

$70^\circ + \angle b = \angle c$
 $\Rightarrow 70^\circ + 50^\circ = \angle c$
 $\angle c = 120^\circ$

$\angle a + \angle b + \angle c = 110^\circ + 50^\circ + 120^\circ = 280^\circ$

03. (A) $\frac{2(x+4)+3(1+2x)}{4} = 0$

$2x + 8 + 3 + 6x = 0$

$8x = -11$

$x = -\frac{11}{8}$

04. (A) $x^2 - 2x - x(x+1) = x^2 - 2x - x^2 - x$
 $= -3x = -3 \times 2025 = -6075$

05. (A) Given $\frac{3x}{4} + x + \frac{x}{2} = 180^\circ$

$$\frac{3x + 4x + 2x}{4} = 180^\circ$$

$$9x = 180^\circ \times 4$$

$$x = 80^\circ$$

06. (A) $\frac{3}{4} \times \text{S.P} = 90\% \text{ of C.P}$

(Since loss = 10%)

$$\Rightarrow \text{S.P} = 120\% \text{ of C.P}$$

$$\Rightarrow \text{S.P} = 1.2 \text{ of C.P}$$

$$\therefore \text{Profit \%} = \frac{1.2\text{C.P} - \text{C.P}}{\text{C.P}} \times 100\%$$

$$= 0.2 \times 100 = 20\%$$

07. (A) $\angle a = 40^\circ$ & $x + 100^\circ = 180^\circ$

$$x = 180^\circ - 100^\circ = 80^\circ$$

$$\text{But } \angle x + \angle a + \angle y = 180^\circ$$

$$40^\circ + 80^\circ + \angle y = 180^\circ$$

$$y = 180^\circ - 120^\circ = 60^\circ$$

08. (B) Given $B : C : D = 2 : 3 : 7 = 2x : 3x : 7x$

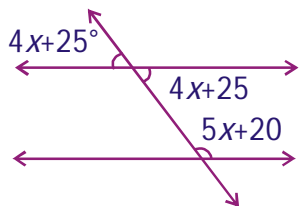
$$\therefore 60^\circ + 2x + 3x + 7x = 360^\circ$$

$$12x = 360^\circ - 60^\circ$$

$$x = \frac{300^\circ}{12} = 25^\circ$$

$$C = 3x = 3 \times 25^\circ = 75^\circ$$

09. (A) Given $l \parallel m \Rightarrow 4x + 25^\circ + 5x + 20^\circ = 180^\circ$



$$9x + 45^\circ = 180^\circ$$

$$9x = 180^\circ - 45^\circ$$

$$9x = 135^\circ$$

$$x = \frac{135^\circ}{9} = 15^\circ$$

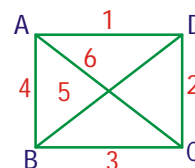
10. (A)

$$\frac{(67.542)^2 - (32.458)^2}{7000 - 3491.6} = \frac{(67.542 + 32.458)(67.542 - 32.458)}{3508.4}$$

$$= \frac{100 \times 35.084}{3508.4}$$

$$= \frac{3508.4}{3508.4} = 1$$

11. (A) Six line segments are formed with 4 points such that no three points are collinear



12. (B) $4^{3.5} : 2^5 = (2^2)^{3.5} : 2^5$

$$= 2^7 : 2^5$$

$$= 2^5 \times 2^2 : 2^5$$

$$= 4 : 1$$

13. (B) Required value = $1000^2 + 345^2 + 655^2 - 2 \times 1000 \times 345 + 2 \times 345 \times 655 - 2 \times 1000 \times 655$

$$= 1000000 + 119025 + 429025 - 690000 + 451950 - 1310000$$

$$= 0$$

14. (A) $(1^3 + 2^3 + 3^3 + \dots + 7^3)^{\frac{3}{2}} = (1 + 8 + 27 + 64 + 125 + 216 + 343)^{-3/2}$

$$= (784)^{\frac{3}{2}} = 28^{2 \times \frac{3}{2}}$$

$$= 28^3 = 21952$$

15. (D) Given $8x + 13x + 45^\circ + 17x + 40^\circ = 180^\circ$

$$38x + 85^\circ = 180^\circ$$

$$38x = 180^\circ - 85^\circ$$

$$38x = 95^\circ$$

$$x = \frac{95^\circ}{38} = \frac{5^\circ}{2} = 2.5^\circ$$

$$\therefore 8x = 8 \times 2.5^\circ = 20^\circ$$

$$13x + 45^\circ = 13 \times 2.5^\circ + 45^\circ = 32.5^\circ + 45^\circ = 77.5^\circ$$

$$17x + 40^\circ = 17 \times 2.5^\circ + 40^\circ = 42.5^\circ + 40^\circ = 82.5^\circ$$

$$\therefore \text{Required sum} = 82.5^\circ + 20^\circ = 102.5^\circ$$

16. (A) Given $a = c = 1$
 Given ab, ba, cd & dc are primes.
 $\therefore ab = 13$ & $ba = 31$
 $cd = 17$ & $dc = 71$

$$\therefore \frac{ab+ba}{cd+dc} = \frac{13+31}{17+71} = \frac{44}{88} = \frac{1}{2}$$

17. (D) Given $AB : BC = 1 : 2$ and $BC : CD = 5 : 8$
 $\therefore AB : BC : CD = 5 : 10 : 16 = 5x : 10x : 16x$
 $\therefore AB : BD = 5x : (10x + 16x) =$
 $5x : 26x = 5 : 26$

18. (C) $144 - \frac{1024}{16} \times 32 - 123$
 $= 144 - 2048 - 123 = -2027$

19. (D) Const.: $AQ \parallel PO$
 $\therefore \angle OPQ + \angle PQA = 180^\circ$
 [\because Sum of the interior angles]
 $\therefore \angle PQA = 70^\circ$
 But $\angle AQR = \angle QRS$
 [\because Alternative angles]
 $\therefore \angle PQA + \angle PQR = 130^\circ$
 $70^\circ + \angle PQR = 130^\circ$
 $\angle PQR = 60^\circ$

20. (C) Given profit = ₹ 175
 Let CP be ₹ x .
 Given 14% of $x = ₹ 175$
 $\frac{14}{100} \times x = ₹ 175$
 $x = ₹ 1250$
 $\therefore CP = ₹ 1250$
 $SP = CP + P = 1250 + 175 = 1425$

21. (D) Given $\sqrt{l^2 + b^2} = 2b$
 Squaring on both sides
 $l^2 + b^2 = 4b^2$
 $l^2 = 4b^2 - b^2$
 $l^2 = 3b^2$
 $l = \sqrt{3b^2} = \sqrt{3}b$
 $\therefore \frac{l}{b} = \sqrt{3}$
 $\therefore l : b = \sqrt{3} : 1$

22. (A) $\angle ABD = 180^\circ - 100^\circ = 80^\circ$
 In $\triangle ABD$, $AB = AD$ $\angle ADB = \angle ABD = 80^\circ$
 In $\triangle ACD$, $x + 25^\circ = 80^\circ$
 $x = 80^\circ - 25^\circ = 55^\circ$

23. (C) In $\triangle RST$, $27^\circ + 100^\circ + \angle S = 180^\circ$
 $\angle S = 180^\circ - 127^\circ = 53^\circ$
 But $\angle P = \angle S$ [\because Alternative angles]
 $\therefore \angle P = 53^\circ$

24. (B) Let the two equal angles be ' x '
 $x + x = 180^\circ$
 $2x = 180^\circ$
 $x = 90^\circ$
 \therefore Each equal angle = 90°

25. (B) $\frac{5}{11} < \frac{1}{2} < \frac{3}{4} < \frac{6}{7}$
 $\frac{-6}{7} < \frac{-3}{4} < \frac{-1}{2} < \frac{-5}{11}$

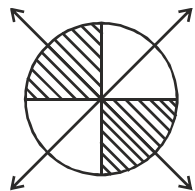
26. (D) 360°

27. (A) $LHS = \left(\frac{13x}{4} - \frac{5}{14}y - \frac{13z}{10} \right)$
 $- \left(\frac{-11}{2}x - \frac{13y}{7} - \frac{12z}{5} \right)$
 $= \frac{13x}{4} - \frac{5}{14}y - \frac{13z}{10} + \frac{11x}{2} + \frac{13y}{7} + \frac{12z}{5}$
 $= \left(\frac{13x}{4} + \frac{11x}{2} \right) + \left(\frac{13y}{7} - \frac{5y}{14} \right) + \left(\frac{12z}{5} - \frac{13z}{10} \right)$
 $= \left(\frac{13x + 22x}{4} \right) + \left(\frac{26y - 5y}{14} \right) + \left(\frac{24z - 13z}{10} \right)$
 $= \frac{35x}{4} + \frac{21y}{14} + \frac{11z}{10}$
 $= \frac{35x}{4} + \frac{3y}{2} + \frac{11z}{10}$

28. (B) $\angle ACB = 45^\circ$

29. (D) $\frac{26}{100} \times 450 - x = \frac{12}{100} \times 150$
 $117 - x = 18$
 $x = 99$

30. (C) It has two lines of symmetry



MATHEMATICS - 2 (MAQ)

31. (A,B,C,D) $-\frac{1}{4} = 0.25$, $-\frac{1}{3} = -0.33$

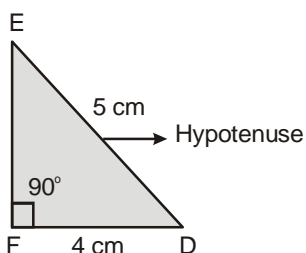
$-\frac{7}{24} = -0.29$ lies between $-\frac{1}{4}$ and $-\frac{1}{3}$

$-\frac{13}{48} = -0.27$ lies between $-\frac{1}{4}$ and $-\frac{1}{3}$

$-\frac{5}{16} = -0.312$ lies between $-\frac{1}{4}$ and $-\frac{1}{3}$

$-\frac{31}{120} = -0.258$ lies between $-\frac{1}{4}$ and $-\frac{1}{3}$

32. (A,B,C,D) $\triangle DEF$ is as shown in the figure.



By Pythagoras' theorem,

$$EF = \sqrt{DE^2 - DF^2}$$

$$= \sqrt{25 - 16} = \sqrt{9} = 3 \text{ cm}$$

By angle sum property,

$$\angle D + \angle E = 180^\circ - \angle F$$

$$= 180^\circ - 90^\circ = 90^\circ$$

33. (A,B,C,D) All the given statements about the triangle are correct.

34. (B,C) $2^{2025} = 2 \times 2 \times 2 \times \dots \times 2$ (2025 times)

It is even number [\because Product of two even numbers]

It is composite number.

35. (B,C,D) $\frac{7x}{2} - \frac{5x}{2} - \frac{20x}{3} = 10$

$$\frac{21x - 15x - 40x}{6} = 10$$

$$-\frac{34x}{6} = 10$$

$$\frac{17x}{3} = -10$$

$$x = -10 \times \frac{3}{17} = -\frac{30}{17}$$

\therefore Option (A) is false, rest of all true.

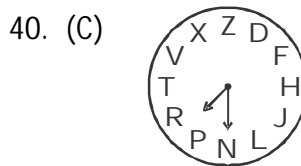
REASONING

36. (B) The first figure rotates 90° ACW, completes the figure and fills interchange.

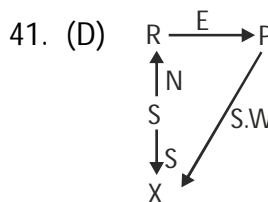
37. (C) Every alternate figure has 4 and 2 dots respectively and two lines forming 90° angle (line \rightarrow) is added at the end in CW direction in each step to form a shape as in the last square.

38. (D) $(3 \times 4) - 8 = 4$; $(2 \times 5) - 4 = 6$; $(4 \times 5) - 9 = 11$

39. (C) Number of lines inside the square and outside at the bottom are the same unlike the others.

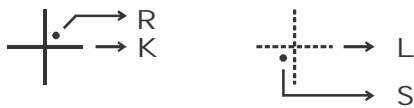


The hour hand will be between P and R at 7: 30.



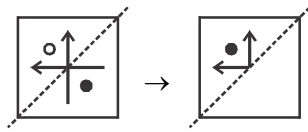
X is in the south-west direction of P.

42. (B)

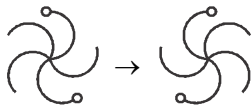


So, the code for must be SK

43. (B)



44. (D)



45. (A)

Bottom layer : $(8 + 1) = 9$;

Middle layer : $(4 + 1) = 5$;

Top layer = 1

Total : $9 + 5 + 1 = 15$

CRITICAL THINKING

46. (B)

| Name | Name | Lives on |
|----------------|----------|-----------|
| Suma | Singer | 5th floor |
| Pavitra | Doctor | 4th floor |
| Meghana | Engineer | 3rd floor |
| Nikita | Artist | 2nd floor |

47. (D)

From 1 and 2 statements 6 is not the correct number.

From 4th statement 7,3, and 8 are not the correct number.

From 5th statement we conclude that "0" is the correct number but in wrong position. So, "0" occupies 1st position (since 0 is one of the numbers in the wrong place from statement 3).

From 1st statement we conclude that 2 is the 3rd digit.

0 _ 2

- From statement 2, since 1 or 4 is in the wrong place, we need to determine which.
- 1 cannot be in the second place. So, 4 occupies 2nd position.

Therefore, the digits are 042.

48. (A)

| | Mr. Red | Mr. Blue | Mr. Green | Mr. Yellow |
|--------|---------|----------|-----------|------------|
| Red | ✗ | | | |
| Blue | ✗ | ✗ | | |
| Green | | ✗ | ✗ | |
| Yellow | | | ✗ | ✗ |

(A) Mr. Red - Yellow, Mr. Blue - Red, Mr. Green - Blue, Mr. Yellow - Green

- Mr. Red (Yellow) - Valid
- Mr. Blue (Red) - Valid
- Mr. Green (Blue) - Valid
- Mr. Yellow (Green) - Valid

(B) Mr. Red - Green, Mr. Blue - Yellow, Mr. Green - Red, Mr. Yellow - Blue

- Mr. Red (Green) - Valid
- Mr. Blue (Yellow) - Valid
- Mr. Green (Red) - Valid
- Mr. Yellow (Blue) - Invalid (Mr. Blue cannot sit on Blue)

(C) Mr. Red - Blue, Mr. Blue - Green, Mr. Green - Yellow, Mr. Yellow - Red

- Mr. Red (Blue) - Invalid (Mr. Red cannot sit on Blue)

(D) Mr. Red - Yellow, Mr. Blue - Green, Mr. Green - Red, Mr. Yellow - Blue

- Mr. Red (Yellow) - Valid
- Mr. Blue (Green) - InValid
- Mr. Green (Red) - Valid
- Mr. Yellow (Blue) - Valid

Therefore, the correct answers :

(A) Mr. Red - Yellow, Mr. Blue - Red, Mr. Green - Blue, Mr. Yellow - Green

49. (D)

$$M \times N - C + F$$

50. (D)

